

## Crystal structure and hydrogen bonding of copiapite

By P. SÜSSE

Mineralogisch-Kristallographisches Institut der Universität Göttingen

(Received 7 September 1971)

### Auszug

Copiapite,  $\text{MgFe}_4[(\text{OH})_2(\text{SO}_4)_6] \cdot 20\text{H}_2\text{O}$ , ist triklin, Raumgruppe  $P\bar{1}$ , mit  $a = 7,342 \text{ \AA}$ ,  $b = 18,818 \text{ \AA}$ ,  $c = 7,389 \text{ \AA}$ ,  $\alpha = 91,45^\circ$ ,  $\beta = 102,15^\circ$  und  $\gamma = 98,85^\circ$ . In der Struktur sind  $\text{Fe}(\text{O},\text{OH},\text{H}_2\text{O})_6$ -Koordinationsoktaeder und Sulfattetraeder zu eindimensional-unendlichen Komplexen parallel  $[101]$  verknüpft.  $\text{Mg}(\text{H}_2\text{O})_6$ -Oktaeder und nicht an Kationen gebundene Wassermoleküle liegen zwischen den Komplexen. Die einzelnen Struktureinheiten sind nur über Wasserstoffbrücken miteinander verknüpft.

### Abstract

The structure of copiapite,  $\text{MgFe}_4[(\text{OH})_2(\text{SO}_4)_6] \cdot 20\text{H}_2\text{O}$ , is triclinic, space group  $P\bar{1}$ , with  $a = 7.342 \text{ \AA}$ ,  $b = 18.818 \text{ \AA}$ ,  $c = 7.389 \text{ \AA}$ ,  $\alpha = 91.45^\circ$ ,  $\beta = 102.15^\circ$ , and  $\gamma = 98.85^\circ$ .  $\text{Fe}(\text{O},\text{OH},\text{H}_2\text{O})_6$  octahedra and sulfate tetrahedra are connected to form one-dimensional infinite complexes along  $[101]$ .  $\text{Mg}(\text{H}_2\text{O})_6$  octahedra and water molecules not bound to cations lie between the complexes. These structural groups are interconnected only by hydrogen bonds.

### Introduction

Copiapite, a greenish-yellow secondary mineral found in the oxidation zone of sulfidic iron-ore deposits, is the commonest of the natural ferric sulfates. It was first described by ROSE (1833). Considered to be monoclinic by LINCK (1889), it was later found to be triclinic by PALACHE *et al.* (1946). The general chemical formula (BERRY, 1947) is  $AB_4[(\text{OH})_2(\text{SO}_4)_6] \cdot 20\text{H}_2\text{O}$ , where  $A$  is usually  $\text{Fe}^{2+}$ , Mg, Cu, Zn and  $B$  is  $\text{Fe}^{3+}$ , Al.

### Experimental

The crystals used for this investigation are from Alcaparrosa, Chile. The cation chemistry was assumed to be  $A = \text{Mg}$  and  $B = \text{Fe}^{3+}$ , which was later confirmed during the structure refinement.

Single-crystal x-ray photographs showed triclinic symmetry. The lattice constants were measured on NaCl-calibrated photographs and refined by the method of least squares. They are in good agreement with those determined earlier on crystals from other localities, as shown in Table 1.

The unit cell has a volume of  $984.4 \text{ \AA}^3$  and contains  $1 \times [\text{MgFe}_4(\text{OH})_2(\text{SO}_4)_6 \cdot 20\text{H}_2\text{O}]$ . The calculated density is  $2.05 \text{ g} \cdot \text{cm}^{-3}$ ; the measured density is  $2.04 \text{ g} \cdot \text{cm}^{-3}$ .

Table 1. Cell constants of copiapites

Cell dimensions	Chuquicamata, Chile, PALACHE <i>et al.</i> (1946)	Alaska, JOLLY and FOSTER (1967)	Alcaparrosa, Chile, this work
<i>a</i>	7.34 Å	7.251 Å	$7.342 \pm .007 \text{ \AA}$
<i>b</i>	18.19	18.161	$18.818 \pm .010$
<i>c</i>	7.28	7.267	$7.389 \pm .004$
$\alpha$	$93^\circ 51'$	$93^\circ 59' 35''$	$91.45 \pm .04^\circ$
$\beta$	$101^\circ 30'$	$102^\circ 17' 16''$	$102.15 \pm .11^\circ$
$\gamma$	$99^\circ 23'$	$97^\circ 57' 46''$	$98.85 \pm .09^\circ$

Intensities were measured with an automated two-circle diffractometer on a square tabular crystal of dimensions  $0.3 \times 0.3 \times 0.07 \text{ mm}$ , rotated about the *a* axis. The reflected Zr-filtered  $\text{MoK}\alpha$  radiation was detected by a scintillation counter. Within the hemisphere out to  $(\sin \theta)/\lambda = 0.55 \text{ \AA}^{-1}$ , 2902 reflections were measured, of which 184 had intensities below the detectable limit and were assigned intensities of one-third the value of the weakest measurable reflection. The intensities were corrected for Lorentz, polarization, and absorption effects.

### Structure determination and refinement

A three-dimensional Patterson synthesis was used to determine approximate positions of the two iron and three sulfur atoms. Through a subsequent structure-factor calculation yielding an *R* value of 46%, correct signs could be found for about two-thirds of the observed *F*'s. They were used to compute a three-dimensional Fourier synthesis, which revealed the positions of all atoms except hydrogen. In the subsequent structure-factor calculation the *R* value dropped to 20%. A full-matrix, least-squares refinement with isotropic temperature

Table 2. Atom parameters of copiapite

Atom	<i>x</i>	<i>y</i>	<i>z</i>
Mg	0	0	0
Fe(1)	0.6861 (2)	0.3326 (1)	0.4944 (2)
Fe(2)	.6833 (2)	.6800 (1)	.8980 (2)
S(1)	.9461 (4)	.7338 (1)	.3113 (3)
S(2)	.7221 (4)	.4200 (1)	.1318 (3)
S(3)	.5945 (4)	.2057 (1)	.1675 (3)
O(1)	.774 (1)	.6993 (4)	.172 (1)
O(2)	.881 (1)	.7607 (4)	.469 (1)
O(3)	.944 (1)	.3248 (4)	.631 (1)
O(4)	.943 (1)	.2103 (4)	.771 (1)
O(5)	.551 (1)	.3702 (4)	.037 (1)
O(6)	.671 (1)	.4905 (4)	.166 (1)
O(7)	.807 (1)	.3917 (4)	.311 (1)
O(8)	.857 (1)	.4254 (4)	.011 (1)
O(9)	.580 (1)	.1272 (4)	.178 (1)
O(10)	.597 (1)	.7757 (4)	.893 (1)
O(11)	.712 (1)	.2317 (4)	.038 (1)
O(12)	.682 (1)	.2406 (4)	.357 (1)
O(13)	.567 (1)	.6562 (4)	.635 (1)
O(14)	.572 (1)	.2788 (4)	.694 (1)
O(15)	.706 (1)	.4262 (4)	.647 (1)
O(16)	.758 (1)	.9491 (5)	.076 (1)
O(17)	.778 (1)	.5834 (4)	.919 (1)
O(18)	.854 (1)	.9923 (5)	.728 (1)
O(19)	.919 (1)	.7206 (4)	.818 (1)
O(20)	.912 (1)	.0976 (5)	.035 (1)
O(21)	.725 (1)	.8934 (5)	.418 (1)
O(22)	.768 (1)	.5601 (4)	.509 (1)
O(23)	.657 (1)	.1007 (5)	.570 (1)

factors brought the *R* value down to 11%. Finally, anisotropic thermal parameters were varied in the least-squares refinement. This led to a final *R* value of 0.096 for all data. Table 2 lists the refined atom parameters and their standard deviations. Mg occupies the special position in the cell origin; all other atoms are in general positions. The thermal parameters and their standard deviations are given in Table 3. Table 4 lists the corresponding root-mean-square amplitudes along principal axes. The temperature factor is defined as  $\exp[-\frac{1}{4}(B_{11}a^{*2}h^2 + B_{22}b^{*2}k^2 + B_{33}c^{*2}l^2 + 2B_{23}b^*c^*kl + 2B_{13}a^*c^*hl + 2B_{12}a^*b^*hk)]$ . The equivalent isotropic temperature coefficients  $B_{iso}$  were computed from

Table 3. *Thermal parameters of atoms in copiapite*

Atom	$B_{11}$	$B_{22}$	$B_{33}$	$B_{23}$	$B_{13}$	$B_{12}$	$B_{iso}$
Mg	1.70(26) Å <sup>2</sup>	2.19(22) Å <sup>2</sup>	2.07(21) Å <sup>2</sup>	0.34(17) Å <sup>2</sup>	0.35(18) Å <sup>2</sup>	0.52(18) Å <sup>2</sup>	1.95 Å <sup>2</sup>
Fe(1)	0.83(07)	1.47(06)	0.71(05)	0.22(04)	0.02(04)	0.21(05)	0.95
Fe(2)	0.48(07)	1.47(06)	1.00(05)	0.24(04)	−0.04(05)	0.18(05)	0.89
S(1)	0.89(12)	1.77(10)	0.93(09)	0.31(07)	0.13(08)	0.15(08)	1.13
S(2)	0.87(12)	1.57(10)	0.97(09)	0.32(07)	0.11(08)	0.11(08)	1.09
S(3)	0.77(12)	1.52(10)	1.20(09)	0.16(07)	0.09(08)	0.24(08)	1.12
O(1)	0.71(36)	2.81(36)	2.41(34)	0.27(27)	0.07(26)	0.01(27)	1.72
O(2)	2.87(42)	2.11(32)	1.18(28)	0.30(24)	0.72(27)	0.72(28)	1.81
O(3)	1.51(38)	1.56(31)	2.96(36)	0.54(26)	0.42(28)	0.64(26)	1.79
O(4)	1.76(40)	2.59(34)	1.76(31)	0.61(25)	0.58(27)	−0.35(28)	1.87
O(5)	0.39(34)	2.65(34)	1.04(27)	0.24(24)	−0.37(23)	−0.04(26)	0.90
O(6)	3.15(44)	1.06(30)	1.88(32)	0.06(24)	0.32(29)	0.44(28)	1.84
O(7)	1.26(37)	1.88(31)	1.06(28)	0.25(23)	0.02(25)	0.22(26)	1.37
O(8)	1.18(37)	3.06(36)	1.32(30)	1.06(26)	0.72(25)	0.15(28)	1.30
O(9)	1.57(39)	1.17(29)	2.69(35)	0.05(25)	0.13(28)	0.30(26)	1.72
O(10)	0.71(34)	1.95(30)	0.88(26)	0.01(22)	−0.07(23)	0.08(24)	1.09
O(11)	1.02(37)	2.61(35)	1.45(30)	0.26(25)	0.38(26)	0.29(27)	1.54
O(12)	1.75(39)	2.06(33)	1.15(28)	0.21(24)	0.14(26)	0.75(27)	1.55
O(13)	1.41(37)	2.00(31)	1.18(28)	0.31(23)	0.51(25)	−0.20(26)	1.41
O(14)	2.11(40)	2.30(33)	1.30(30)	−0.03(25)	0.76(27)	0.19(28)	1.74
O(15)	2.05(39)	2.22(33)	1.51(30)	0.41(25)	0.28(26)	0.52(27)	1.87
O(16)	2.02(43)	3.35(41)	2.87(38)	−0.07(31)	0.59(31)	−0.31(32)	2.69
O(17)	1.22(37)	1.84(31)	2.52(34)	0.76(26)	0.44(27)	0.60(26)	1.64
O(18)	4.49(55)	3.30(43)	2.88(40)	0.41(33)	0.30(37)	1.31(38)	3.42
O(19)	1.30(38)	2.62(35)	2.35(34)	0.63(27)	0.75(27)	−0.11(27)	1.85
O(20)	4.37(54)	2.07(36)	3.62(43)	0.25(31)	1.35(38)	0.96(34)	3.04
O(21)	3.43(49)	2.70(38)	3.09(40)	0.11(31)	0.51(35)	0.36(33)	3.10
O(22)	3.16(45)	1.91(33)	2.04(33)	0.35(26)	0.95(30)	0.35(29)	2.22
O(23)	3.70(52)	2.78(39)	3.37(42)	1.25(32)	0.51(36)	0.53(34)	3.11

Crystal structure and hydrogen bonding of copiapite

Table 4. *Parameters for the ellipsoids of vibration*

Atoms	Root-mean-square amplitudes along the principal axes	Angles with the reciprocal lattice vectors		
		a*	b*	c*
Mg	.14 Å	29.4°	107.4°	67.9°
	.16	66.1	61.1	133.8
	.17	74.0	34.7	51.9
Fe(1)	.11	37.7	78.0	114.7
	.14	86.6	13.3	76.2
	.09	52.5	95.7	28.8
Fe(2)	.14	91.9	156.3	113.9
	.12	72.9	66.3	142.4
	.07	17.2	89.1	62.8
S(1)	.11	41.4	72.2	116.9
	.15	90.7	18.5	73.5
	.10	48.6	94.8	32.3
S(2)	.15	86.2	154.6	111.7
	.11	48.0	65.1	120.2
	.10	42.3	94.6	38.6
S(3)	.14	97.2	166.3	106.2
	.13	77.3	76.3	151.5
	.10	14.6	90.6	67.2
O(1)	.20	86.7	152.4	114.6
	.18	88.8	65.5	150.7
	.09	3.5	78.1	75.0
O(2)	.11	87.6	85.5	164.0
	.16	105.4	25.0	88.6
	.19	15.6	65.5	74.1
O(3)	.20	96.6	104.8	166.3
	.11	129.3	49.3	103.3
	.15	40.1	44.4	93.0
O(4)	.20	70.0	145.8	103.3
	.12	53.3	57.6	120.7
	.16	43.6	80.1	34.0

Table 4. (Continued)

Atoms	Root-mean-square amplitudes along the principal axes	Angles with the reciprocal lattice vectors		
		a*	b*	c*
O(5)	.13 Å	67.0°	74.5°	141.8°
	.19	94.5	17.7	78.9
	.05	23.5	81.6	54.0
O(6)	.20	16.4	82.9	93.8
	.11	87.7	7.2	87.2
	.15	73.8	88.8	4.7
O(7)	.14	37.4	69.2	111.8
	.16	94.7	21.3	74.1
	.11	53.0	94.1	27.5
O(8)	.21	93.3	158.0	112.9
	.07	58.2	68.8	113.5
	.14	32.0	95.5	50.2
O(9)	.19	80.6	87.8	158.0
	.12	96.6	16.0	90.4
	.14	11.5	74.2	68.0
O(10)	.12	60.4	85.6	137.9
	.16	91.3	10.7	89.9
	.09	29.6	80.2	47.9
O(11)	.11	19.4	83.8	96.7
	.18	85.2	7.3	82.0
	.13	71.3	93.8	10.5
O(12)	.14	57.0	119.8	118.2
	.12	120.9	76.6	151.7
	.17	48.5	33.3	88.0
O(13)	.17	67.5	147.3	93.6
	.10	58.7	66.1	130.6
	.14	40.2	69.0	40.8
O(14)	.11	74.7	93.5	151.7
	.18	121.1	43.2	108.6
	.16	35.5	47.0	69.5

Table 4. (Continued)

Atoms	Root-mean-square amplitudes along the principal axes	Angles with the reciprocal lattice vectors		
		$\mathbf{a}^*$	$\mathbf{b}^*$	$\mathbf{c}^*$
O(15)	.16	34.2	101.3	105.7
	.13	108.7	71.1	155.0
	.17	62.4	22.2	71.1
O(16)	.19	93.2	101.6	166.6
	.22	109.9	30.9	102.2
	.15	20.2	61.8	84.4
O(17)	.11	34.0	113.8	73.6
	.14	58.8	41.8	113.0
	.19	77.8	58.0	28.8
O(18)	.25	24.7	66.1	96.6
	.18	114.6	57.2	136.5
	.20	88.4	42.6	47.2
O(19)	.11	32.5	65.6	104.9
	.17	122.4	71.9	146.1
	.20	91.3	31.2	60.3
O(20)	.20	71.3	80.5	147.7
	.15	96.6	16.6	85.5
	.24	19.9	76.5	58.1
O(21)	.21	31.4	93.5	106.7
	.20	115.0	78.8	158.5
	.18	72.3	11.8	76.9
O(22)	.16	87.9	140.5	127.7
	.14	78.3	50.7	133.6
	.20	11.9	86.3	67.2
O(23)	.24	68.1	118.6	131.6
	.15	93.9	39.9	126.3
	.21	22.3	64.8	62.7

hypothetical spheres of vibration having the same volume as the corresponding ellipsoids. The observed and calculated structure factors are compiled in Table 5.



Table 5. (Continued)

h k l		F <sub>o</sub>	F <sub>c</sub>	h k l		F <sub>o</sub>	F <sub>c</sub>	h k l		F <sub>o</sub>	F <sub>c</sub>	h k l		F <sub>o</sub>	F <sub>c</sub>									
1	3	-1	131.9	127.0	3	15	-1	36.3	-35.9	6	5	-1	14.0	-14.3	2	20	2	14.1	21.2	5	7	2	12.4	14.8
4			-117.8		16			14.1	11.4	6			22.3	-23.2	-1			22.6	31.1	8			9.5	11.5
5			37.4	33.3	17			32.5	31.9	7			51.8	51.4	-2			36.9	45.8	9			10.8	-6.3
6			15.4	18.5	18			13.6	-12.5	8			5.3	-5.6	-3			11.2	-15.2	10			4.5	-10.7
7			47.9	-46.8	-1				-54.5	9			10.4	9.2	-4			27.7	28.8	11			10.0	-17.5
8			25.2	22.7	-2				23.9	10			2.1	2.6	-5			19.6	-19.6	12			7.4	-7.8
9			59.1	56.4	-3				41.1	11			14.8	-14.8	-6			84.0	90.4	13			25.8	29.9
10			56.6	-57.2	-4			10.3	8.4	12			2.7	-2.3	-7			2.9	-1.2	-1			22.6	-22.1
11			48.9	48.9	-5			35.5	34.4	-1				-16.3	-8			19.0	-18.6	-2			70.4	69.1
12			76.9	78.3	-6			4.0	4.7	-2				51.0	-9			50.3	53.2	-3			2.8	4.2
13			35.1	-34.8	-7			28.0	-28.3	-3				20.3	-10			15.1	-13.8	-4			38.0	-35.8
14			31.6	35.5	-8			25.0	26.2	-4				8.4	-11			12.7	-11.7	-5			19.9	23.8
15			28.3	32.9	-9			8.5	-6.4	-5			22.8	24.3	-12			5.3	-5.5	-6			32.2	28.9
16			60.1	-61.8	-10			9.8	6.8	-6			31.4	32.1	-13			58.6	62.7	-7			24.9	25.4
17			20.1	16.6	-11			13.3	-9.9	-7			29.5	-31.7	-14			21.9	-16.6	-8			34.1	-33.0
18			41.3	43.0	-12			30.0	26.5	-8			6.8	6.5	-15			54.7	-52.5	-9			2.8	-1.6
19			23.1	-19.9	-13			28.8	26.2	-9			7.1	0.8	-16			53.1	49.3	-10			11.3	13.4
20			7.2	-8.1	-14			25.3	24.8	-10			6.7	3.8	-17			15.8	-13.1	-11			7.5	2.4
21			24.6	28.3	-15			12.7	-13.1	-11			3.4	4.8	-18			15.8	12.6	-12			7.2	11.8
-1			150.0		-16			2.8	1.5	0	0	2	57.8	49.7	-19			7.0	1.2	-13			15.5	-15.8
-2			15.2	-9.1	-17			17.9	12.8	1			155.3	-149.3	-20			21.9	-20.6	-14			3.8	4.6
-3			3.8	-1.5	-18			16.8	13.8	2			58.5	56.2	-21			14.3	15.6	-15			2.7	1.4
-4			73.2	68.6	-19			10.1	4.9	3			32.8	37.0	-22			8.9	12.6	-16			22.7	25.5
-5			104.1	-99.5	-20			2.7	1.4	4			55.8	-50.9	-23			42.7	41.8	-17			2.7	2.5
-6			64.2	61.5	4	0	-1	21.9		5			37.1	-37.5	1			38.4	-38.4	6	0	2	26.1	24.1
-7			135.7	122.9	1			69.2	-66.0	6			66.2	63.1	2			6.0	-1.7	1			9.4	14.8
-8			95.6	-90.1	2			36.2	33.8	7			20.8	-20.0	3			94.0	93.5	2			13.5	-12.2
-9			25.8	25.0	3			53.8	54.1	8			19.7	-21.5	4			75.5	-74.1	3			9.3	8.0
-10			10.1	11.6	13			85.6	-85.9	9			131.7	129.3	-5			15.6	-7.6	4			22.1	-22.8
-11			13.1	11.3	5			69.3	72.8	10			79.8	-80.6	6			97.4	94.7	5			5.6	1.3
-12			7.4	-8.9	6			32.9	31.5	11			31.5	-31.9	7			76.2	-72.0	6			42.0	40.8
-13			37.2	37.3	7			78.2	-80.4	12			43.4	44.3	8			21.7	21.8	7			52.2	-52.6
-14			40.6	-41.0	8			30.1	29.1	13			8.8	-7.1	9			94.3	92.4	8			7.2	-0.9
-15			19.9	-19.8	9			21.7	21.6	14			3.9	5.1	10			22.7	-22.5	9			31.1	-34.8
-16			36.5	34.9	10			16.5	-17.3	15			22.2	-21.9	11			19.8	-21.3	10			8.1	-7.2
-17			11.4	-6.1	11			24.3	-23.4	16			6.9	-5.5	12			42.5	41.0	11			2.7	-2.2
-18			8.4	-7.9	12			4.7	-2.9	17			9.8	-12.8	13			2.2	1.7	-1			6.9	7.3
-19			15.0	11.6	13			13.0	14.9	18			54.9	59.6	14			16.3	-18.9	-2			71.0	-69.7
-20			4.1	6.5	14			4.6	3.8	1	0	2	2.2	-4.1	15			33.1	35.8	-3			59.2	55.2
-21			7.3	0.1	15			24.2	25.7	1			42.5	45.2	16			16.5	-16.2	4			29.1	27.8
-22			7.5	7.9	16			25.7	-28.6	2			92.2	92.0	17			16.9	-16.7	0	1	-2	114.5	109.2
2	0	-1	16.0		-1			89.9		3			73.2	-77.2	-1			81.6	82.4	2			9.3	3.5
3			87.1	69.1	-2			-52.9	1	4			25.1	23.2	-2			34.6	-33.1	3			49.6	49.7
4			50.2	60.8	-3			11.0		5			10.0	-9.5	-3			91.1	-89.8	4			9.1	-89.8
5			49.5	-49.5	-4			42.0	45.1	6			21.7	-23.9	-4			36.0	-35.7	5			7.4	7.6
6			48.9	45.1	-5			48.3	-49.1	7			43.4	43.7	-5			62.2	-63.0	6			50.6	-43.5
7			34.0	29.9	-6			26.1	26.8	8			39.0	-42.9	-6			100.6	95.6	7			47.0	-45.3
8			6.6	7.5	-7			75.5	76.2	9			21.9	25.6	-7			15.6	11.8	8			43.9	-44.5
9			8.8	-8.7	-8			83.0	-85.1	10			36.6	43.1	-8			45.8	-43.1	9			24.5	
10			5.2	-5.8	-9			6.8	6.1	11			17.9		-9			38.9	38.2	10			26.3	21.4
11			41.7	39.1	-10			69.1	71.9	12			-20.5		-10			77.8	77.0	11			25.9	-23.8
12			49.4	49.2	-11			37.0	-39.7	13			13.1	-20.5	-11			2.8	3.5	12			60.3	58.7
13			12.2	-11.6	-12			23.3	-22.6	14			21.2	-21.6	-12			21.2	-19.2	13			10.8	-11.4
14			22.4	-18.4	-13			40.0	42.9	15			16.1	-12.4	-13			34.4	34.5	14			53.3	-56.2
15			10.1	4.8	-14			25.5	-26.4	16			10.7	9.5	-14			51.7	-51.0	15			10.6	-7.0
16			43.4	42.9	-15			16.1	-17.3	17			18.6	21.2	-15			42.1	41.8	16			4.8	11.0
17			8.3	-2.7	-16			60.8	61.1	18			21.8	-23.4	-16			18.5	14.8	17			16.3	20.2
18			6.1	-1.3	-17			6.2	-2.3	19			10.2	19.8	-17			20.3	-16.8	18			25.1	-31.1
19			15.9	-17.2	-18			24.1	-25.2	20			17.8	14.2	-18			13.0	11.7	19			5.6	12.3
20			16.0	17.4	-19			23.3	25.6	-1			12.2	-14.5	-19			5.0	3.5	20			13.2	16.7
21			14.0	-10.1	5	0	-1	0.5		-2			87.9	93.3	-20			14.6	10.2	21			2.7	-2.6
22			4.9	0.7	1			35.8	35.3	-3			71.2	-75.3	4	0	2	35.8	-31.2	1	0	-2	40.4	-38.5
23			13.6	15.9	2			2.9	-4.9	-4			21.4	-18.7	1			54.6	54.8	1			14.7	17.6
-1			27.6	3	3			3.0	3.2	-5			76.6	76.5	2			83.2	84.9	2			71.6	-67.4
-2			7.3	4	4			10.7	-11.7	-6			42.8	-42.8	3			64.6	-66.8	3			45.4	-38.0
-3			81.9	-66.7	5			8.7	-3.0	-7			2.1	-0.7	4			31.4	27.8	4			97.1	93.2
-4			61.7	-61.0	6			47.3	45.2	-8			27.1	27.0	5			41.8	47.7	5			49.1	-45.4
-5			59.7	61.5	7			48.0	-48.9	-9			9.6	12.4	-6			17.0	-17.2	6			7.0	-7.3
-6			66.5	59.3	8			23.6	-26.6	-10			13.5	-11.9	7			17.3	18.5	7			17.4	13.1
-7			51.8	9	9			24.4	24.6	-11			8.5	-4.8	8			11.3	-11.5	8			3.0	4.8
-8			99.9	93.7	10			2.8	4.3	-12			6.3	-7.2	9			2.8	1.3	9			50.7	49.8
-9			62.1	60.4	11			5.6	5.4	-13			37.8	-38.6	10			0.1	10.8	10			7.5	-10.0
-10			19.6	-13.4	12			10.3	12.0	-14			65.8	62.0	11			6.5	4.6	11			66.2	-68.9
-11			53.8	13	13																			

Table 5. (Continued)

h	k	l	F <sub>o</sub>	F <sub>c</sub>	h	k	l	F <sub>o</sub>	F <sub>c</sub>	h	k	l	F <sub>o</sub>	F <sub>c</sub>	h	k	l	F <sub>o</sub>	F <sub>c</sub>	h	k	l	F <sub>o</sub>	F <sub>c</sub>
1	-18	-2	4.6	-13.2	4	15	-2	36.0	42.0	1	5	3	40.3	47.8	3	-10	3	31.6	28.0	1	2	-3	20.5	16.4
-19	10.0	-14.3	-1	1.7	-1.5	6	10.6	-13.5	-11	44.9	46.3	3	32.0	29.0										
-20	20.6	17.2	-2	19.1	-16.8	7	30.5	34.1	-12	46.7	-44.3	4	65.2	-61.5										
-21	7.4	-0.8	-3	29.6	29.1	8	17.4	17.5	-13	27.4	25.0	5	30.0	28.5										
2	0	-2	41.3	-36.3	-4	22.1	21.2	9	12.2	13.7	-14	8.6	4.1	6	27.7	25.4								
1	12.2	13.5	-5	75.2	74.5	10	23.1	-30.0	-15	40.9	-38.9	7	44.7	-42.8										
2	126.8	118.3	-6	23.3	22.0	11	17.4	17.0	-16	24.1	50.2	8	5.5	-5.2										
3	116.8	-110.7	-7	17.4	17.6	12	25.1	-30.0	-18	30.5	-30.0	9	31.1	31.0										
4	19.6	16.0	-8	15.6	-14.1	13	17.8	-1.0	-19	5.7	0.3	10	10.0	9.2										
5	111.8	102.6	-9	49.2	54.7	14	6.5	6.9	4	0	3	9.1	4.7	11	11.1	-10.3								
6	50.6	-49.3	-10	42.2	-47.5	15	13.8	16.0	1	6.2	6.9	12	31.2	32.6										
7	16.5	-11.2	-11	29.0	30.4	16	1.8	13.2	2	37.0	40.2	13	19.5	-23.5										
8	112.6	106.7	-12	19.3	-21.8	17	6.8	-4.7	3	49.3	-51.3	14	16.3	17.8										
9	36.1	-34.5	-13	28.3	26.1	18	13.1	12.5	4	13.4	16.9	15	30.2	27.0										
10	31.3	-29.6	-14	6.4	5.4	19	3.8	2.7	5	32.6	34.9	16	6.2	-4.8										
12	6.0	-6.3	-15	11.2	10.9	-4	14.3	12.2	6	4.9	-5.9	17	38.7	-38.5										
13	51.3	-52.8	-16	5.7	6.0	-5	7.6	-1.2	7	19.2	-17.4	18	16.4	10.5										
14	46.9	40.4	-17	9.1	9.4	-6	6.8	-4.7	8	28.1	-27.9	19	10.2	12.7										
15	13.1	-11.5	-18	20.8	19.0	-7	2.9	3.0	9	39.8	39.8	20	7.0	-10.1										
16	14.2	14.6	5	1	-2	5.7	6.0	-8	21.9	18.3	-2	59.7	-59.4	-5	88.6	-87.2								
17	20.1	19.2	2	91.3	88.9	-6	6.8	-4.7	10	4.5	3.5	-3	27.2	-25.1	-6	75.6	72.1							
18	21.6	-23.0	3	35.6	34.4	-7	10.2	7.9	11	22.9	23.2	-2	19.5	17.2	-7	60.9	62.3							
19	5.4	-5.6	4	20.8	19.0	-8	2.9	3.0	12	28.1	-27.9	-3	16.0	16.3	-8	66.8	-65.3							
20	30.7	27.6	5	29.5	29.5	-9	21.9	18.3	-1	39.8	39.8	-4	15.1	12.8	-9	15.1	12.8							
21	2.7	3.0	6	13.0	-9.4	-10	4.5	3.5	-2	59.7	-59.4	-5	88.6	-87.2	-10	88.6	-87.2							
-1	14.2	-12.2	7	2.8	-2.6	-11	7.6	8.0	-3	27.2	-25.1	-6	75.6	72.1	-11	44.6	-43.1							
-2	4.3	-0.1	8	36.4	34.4	-12	45.8	45.7	-4	19.5	17.2	-7	60.9	62.3	-12	17.1	18.4							
-3	19.0	15.9	9	5.8	-11.0	-13	16.1	-19.5	-5	37.1	46.2	-8	66.8	-65.3	-13	19.6	19.6							
-4	27.7	-22.1	10	33.8	-33.2	-14	44.7	-43.3	-6	28.7	-28.1	-9	57.8	58.9	-14	56.8	-62.0							
-5	12.6	8.3	11	59.8	65.3	-15	53.5	51.2	-7	41.9	-45.0	-10	57.8	58.9	-15	28.6	32.2							
-6	10.5	-9.6	12	9.8	-8.0	-16	15.2	16.9	-8	57.1	60.3	-11	44.6	-43.1	-16	44.6	-43.1							
-7	17.7	16.0	13	22.4	-24.4	-17	17.0	-12.7	-9	5.9	9.4	-12	17.1	18.4	-17	3.7	2.6							
-8	17.7	16.0	14	20.9	26.0	-18	3.5	-5.3	-10	8.1	-6.7	-13	19.6	19.6	-18	35.2	36.0							
-9	93.4	-89.4	15	6.1	-6.4	-19	9.6	8.3	-11	19.2	-20.4	-14	56.8	-62.0	-19	8.6	-11.5							
-10	99.3	96.1	-1	46.7	-20	13.2	11.9	-13	16.7	15.9	-17	44.6	-43.1	-20	25.7	25.8								
-11	2.9	1.4	-2	4.1	9.4	-21	10.6	15.1	-14	3.7	-3.1	-18	3.7	2.6	-21	25.7	25.8							
-12	50.1	-47.9	3	5.6	1.4	2	0	1	-15	22.0	23.7	-19	35.2	36.0	-22	25.7	25.8							
-13	31.0	30.0	-4	55.2	61.8	1	17.9	24.6	-16	12.9	-13.3	-20	8.6	-11.5	-23	25.7	25.8							
-14	48.7	47.0	-5	9.1	10.4	2	-64.8	5	0	3	32.9	2	0	-3	25.7	25.8								
-15	10.2	-10.8	-6	63.1	-65.0	3	89.9	1	13.7	-14.2	1	25.7	25.8	-24	25.7	25.8								
-16	23.0	-22.7	-7	63.5	65.3	4	5.4	-8.8	2	16.2	-15.4	2	40.7	39.0	-25	25.7	25.8							
-17	20.8	22.0	-8	46.1	46.5	5	46.8	-82.7	3	54.6	53.0	3	98.1	94.1	-26	25.7	25.8							
-18	22.0	-19.4	-9	84.5	-88.1	6	38.8	4	3.2	4.6	4	15.1	-12.8	-27	25.7	25.8								
-19	2.7	4.0	-10	46.8	48.1	7	48.8	5	50.6	-49.9	5	49.7	-47.1	-28	25.7	25.8								
-20	14.9	13.5	-11	27.5	30.8	8	-54.6	6	18.3	19.5	6	40.2	41.2	-29	25.7	25.8								
-21	17.6	-14.1	-12	16.7	-14.5	9	5.6	5.6	7	34.8	33.9	7	31.8	26.5	-30	25.7	25.8							
-22	8.0	8.3	-13	15.1	18.4	10	10.3	10.3	8	27.8	-30.7	8	41.4	-40.4	-31	25.7	25.8							
3	0	-2	20.6	19.5	-14	19.9	23.3	11	22.8	-24.0	9	12.4	-12.1	-32	25.7	25.8								
1	52.3	46.4	-15	17.5	-16.9	12	21.4	10	10.6	13.4	10	31.6	-29.0	-33	25.7	25.8								
2	55.8	-55.0	-16	7.7	-4.2	13	8.1	17.4	11	6.8	-15.7	11	41.8	38.0	-34	25.7	25.8							
3	125.6	120.7	-17	11.1	15.9	14	-33.6	-1	35.8	-35.3	12	60.8	58.3	-35	25.7	25.8								
4	63.5	61.4	-18	12.5	-15.9	15	13.9	20.9	-2	31.3	31.7	13	56.1	-47.4	-36	25.7	25.8							
5	3.4	-0.7	-19	6.5	20.5	16	9.0	16.4	-3	45.6	44.5	14	16.6	-21.1	-37	25.7	25.8							
6	36.6	-31.4	6	0	-2	46.6	48.5	17	9.2	-10.2	-4	35.4	31.6	-38	25.7	25.8								
7	31.5	29.0	1	53.0	-51.4	18	9.0	9.5	-5	6.2	6.7	16	9.7	3.5	-39	25.7	25.8							
8	15.5	15.0	2	11.2	-13.3	19	18.1	19.1	-6	40.3	38.7	17	27.2	-25.5	-40	25.7	25.8							
9	19.6	-18.2	3	5.9	5.6	-2	31.0	-81.8	-7	40.9	-38.0	18	9.2	8.2	-41	25.7	25.8							
10	12.0	-6.3	4	45.7	44.8	-3	40.9	50.0	-8	2.8	1.3	19	8.7	8.8	-42	25.7	25.8							
11	20.2	-20.1	5	8.7	8.8	-4	4.4	-1.1	-9	23.0	21.0	20	27.1	-25.2	-43	25.7	25.8							
12	43.4	43.4	6	47.7	-47.0	-5	17.8	-19.7	-10	15.7	-7.7	-1	97.7	-93.0	-44	25.7	25.8							
13	33.5	33.6	7	36.1	38.8	-6	63.4	74.5	-11	23.7	-23.3	-2	27.0	-24.9	-45	25.7	25.8							
14	9.9	-10.4	8	10.1	14.4	-7	33.7	-37.9	-12	50.2	52.7	-3	16.3	14.0	-46	25.7	25.8							
15	3.9	-8.0	9	10.1	6.4	-8	7.8	-8.2	-13	17.3	-17.5	-4	20.1	-16.7	-47	25.7	25.8							
16	9.9	-5.2	10	14.3	-15.5	-9	92.1	99.8	-14	29.8	-31.2	-5	16.2	-14.7	-48	25.7	25.8							
17	18.9	20.9	11	2.7	2.7	-10	53.8	-56.6	-15	21.2	24.1	-6	2.7	-1.2	-49	25.7	25.8							
-1	30.5	-35.5	12	8.5	6.4	-11	13.1	10.3	-16	8.7	-12.9	-7	31.2	32.4	-50	25.7	25.8							
-2	54.8	54.7	-1	5.1	3.8	-12	64.4	68.1	6	0	3	3.9	7.9	-9	23.7	-23.0	-51	25.7	25.8					
-3	17.7	-15.5	-2	-17.7	-14	9.4	12.7	-14	6.6	6.3	2	7.7	-8.1	-10	15.5	-12.1	-52	25.7	25.8					
-4	4.3	-5.9	-3	39.4	-42.2	-16	8.5	-1.0	3	5.9	2.8	-11	2.9	0.0	-53	25.7	25.8							
-5	17.0	-14.4	-4	22.7	26.2	-17	28.1	-29.2	4	6.6	-2.9	-12	11.1	8.4	-54	25.7	25.8							
-6	61.5	61.1	-5	19.2	21.7	-18	21.3	22.0	5	10.6	15.0	-13	23.7	-19.7	-55	25.7	25.8							
-7	15.7	16.6	-6	2.9	5.1	-19	12.5	13.7	6	2.8	2.7	-14	30.0	28.4	-56	25.7	25.8							
-8	30.9	-30.2	-7	10.9	-12.2	-20	5.6	0.5	7	5.1	-1.2	-15	3.1	3.5	-57	25.7	25.8							
-9	47.8	47.1	-8	3.2	-2.9	-21	3.4	10.6	8	8.5	-9.4	-16	15.5	-13.8	-58	25.7	25.8							
-10	12.3	-12.3	-9	8.6	15.0	3	0	3	9	-1.2	-1.2	-17	21.5	16.4	-59	25.7	25.8							
-11	3.6	-4.9	0	34.2	-37.3	1	23.5	-21.9	10	24.1	23.9	-18	8.2	8.6	-60	25.7	25.8							
-12	23.8	22.1	0	49.3	-46.9	2	3.0	-1.5	0	-3	94.8	-19	5.7	4.0	-61	25.7	25.8							
-13	18.1	-16.6	1	101.7	96.8	3	25.7	24.3	2	42.2	-40.9	-20	3.6	8.1	-62	25.7	25.8							
-14	2.8	0.0	2	55.3	55.6	4	33.5	35.2	3	14.8	-15.1	-21	17.9	-19.7	-63	25.7	25.8							
-15	21.1	19.8	3	16.2	16.7	5	3.1	9.7	4	3.9	4.2	3	0	-3	41.3	-41.5	-64	25.7	25.8					
-16	10.8	-10.4	4	32.2	32.5	6	30.1	-28.6	5	34.2	31.7	1	80.1	78.4	-65	25.7	25.8							
-17	3.4	1.2	5	50.9	-49.0	7	6.5	5.6	6	35.7	-35.4	2	50.3	-46.8	-66	25.7	25.8							
-18	57.1	60.2	6	11.1	9.1	8	31.6	31.9	7	46.2	47.1	3	49.4	-46.9	-67	25.7	25.8							
-19	14.4	-14.3	7	71.3	68.8	9																		



